$$A = p_1 x + p_2 x^2 + \dots + p_n x^n$$

Then first solve for x and substitute $(1+r)^{-1} = x$ , to find the value of r

# **Chapter 11 Multi Variables and their Functions**

## **Understanding Surfaces and Distance**

For a 3 dimensional figure, the general equation for a plane in space is given by: px + qy + rz = s

Now let us see its economical use,

We can consider each plane or axis to represent a product, then the space is called budget plane, where p, q and r are cost of goods/unit and s is the total value.

Now for a 3D space, we can find the distance between any 2 points on the space,

The formula is given for two point  $(p_1, q_1, r_1)$  and  $(p_2, q_2, r_2)$ 

The distance is given by distance =  $\sqrt{(p_1, -p_2)^2 + (q_1 - q_2)^2 + (r_1 - r_2)^2}$ 

Now the equation for a sphere is given for a center (u,v,w) and radius r

$$(x-u)^2 + (y-v)^2 + (z-w)^2 = r^2$$

# **Chapter 12 Comparative Statistics**

## A peek into General Cases:

For partial derivatives when we know z = f(x, y) and c is a constant

$$F(x,y,z) = c \implies z'_x = -\frac{F'_x}{F'_B}, \ z'_y = -\frac{F'_y}{F'_B} \ for \ F'_B \neq 0$$

Now for a more general case,

$$F(x_1,x_2,...,x_n,z) = \frac{\partial F/\partial x_i}{\partial F/\partial z}$$
, where  $t=1,2,....,n$ 

#### **Understanding Linear Approximation**

The Linear approximation to f(x) about  $(x_0, y_0)$  is given by the formula

$$f(x,y) \approx f(x_o, y_o) + f'_1(x_o, y_o)(x - x_o) + f'_2(x_o, y_o)(y - y_o)$$

Where,  $f_1^i(x_o, y_o)$ , stands for first derivative of  $(x_o, y_o)$  in terms of x and  $f_2^i(x_o, y_o)$  stands for the first derivative of  $(x_o, y_o)$ , in terms of y.

Now one can generalize the above equation to re-write it for functions of several variables Linear approximation to  $z=f(x)=f(x_1,\dots,x_n)$  about  $x^0=(x_1^0,\dots,x_n^0)$ 

$$f(x) \approx f(x^0) + f'_1(x^0)(x - x^0) + \dots + f'_n(x^0)(x_n - x_n^0)$$

Again  $f_n(x^0)$  stands for the first derivative in terms of the nth variable in the equation

### Tangent Planes:

Tangent plane to the graph of z = f(x,y) at the point (a,b,c), with c = f(a,b) has the equation  $z - c = f'_1(a,b)(x-a) + f'_2(a,b)(y-b)$ 

### **Understanding Differentials**

For a = f(b,c) at a point (b,c) the differential will be a = f(b,c)  $da = f'_1(b,c)db + f'_2(b,c)dc$ 

Where db and dc mean differentiation of b and c respectively

## **Understanding the systems of Equations**

- 1. Finding the Number of Degree of Freedom: (The counting Rule)
  - First count the number of variables or n, and then how many number of 'independent' equations are there or i,
  - Now if n>i then n-i is the number of degree of freedom
  - If n<i, then there is no solution to that system
- 2. For a system of equation if we say that it has n number of variables then it will have P number of degree of freedom
  - P is the number of variables that can be chosen freely
  - And n-p is the number of variables whose value can be found when the value of p is decided upon (these are depended on the value of the p)

#### **Basics of Differentiating Systems of Equation**

The First step is to differentiate both side of the equation with respect to their variables, Example: 2a + 2b = 3x - 2y then it would be 2da + 2db = 3dx - 2dy

Next step would be to find the values of da and db in terms of dx and dy by using the two equations.

Next step is to find  $a'_x$  and  $b'_x$  also  $a'_y$  and  $b'_y$ .

just remember that if the equation for da looks like da=3dx+4dy then the result would be simply  $a'_x=3$  and  $a'_y=4$ 

Then you can just substitute the points given to find the exact values